

# RAMAKRISHNA MISSION VIDYAMANDIRA

(Residential Autonomous College affiliated to University of Calcutta)

B.A./B.Sc. FOURTH SEMESTER EXAMINATION, JUNE 2022

SECOND YEAR (BATCH 2020-23)

CHEMISTRY (HONOURS)

Paper : VIII [CC8]

Date : 21/06/2022

Time : 11.00 am – 1.00 pm

Full Marks : 50

[Attempt one question from each unit]

## Unit : I

[14 marks]

1. a) Two ideal gases are at the same T but at different P. If  $n_A$  moles of gas A and  $n_B$  moles of gas B are mixed isothermally, what will be the  $\Delta_{\text{mix}}G$ ?
  - b) Calculate the  $\Delta_{\text{mix}}G$ ,  $\Delta_{\text{mix}}H$  and  $\Delta_{\text{mix}}S$  at 25°C and 1 atm pr, - when 10 moles of Ne are mixed with 20 moles of equimolar mixture of Ne and He.
  - c) A gas obeys the equation of state  $P(V_m - b) = RT$ . For this gas,  $b = 0.0391 \text{ dm}^3 \text{ mol}^{-1}$ . Calculate  $f$  and  $\phi$  (ratio of  $f$  and  $P$ ) for the gas at 1000°C and 1000 atm. Also calculate  $\mu_{\text{real}} - \mu_{\text{ideal}}$ .
  - d) By increasing the number of moles of one of the components of the mixture at constant T and P, its  $\mu$  increases, while, simultaneously,  $\mu$  for other components decrease. Explain with expression of rate of change of  $\mu$  with number of moles.2. [3+3+4+4]
2. a) How does the  $\Delta_{\text{mix}}G/nRT$  and  $\Delta_{\text{mix}}H$  vary with mole fraction? (Show by qualitative plot)
  - b) Show that the molar free energy of mixing in a binary ideal gas mixture is minimum when two gases are present in the equimolar ratio, i.e  $x_1 = x_2 = 1/2$ .
  - c) True pressure is the geometric mean of the fugacity and the ideal pressure. Explain.
  - d) Use Gibbs-Duhem equation to show that  $\mu_i = \left( \frac{\partial E}{\partial n_i} \right)_{S,V,n_{j \neq i}}$ . And comment on the fact that this does not represent partial molar internal energy. [4+3+3+4]

## Unit : II

[14 marks]

3. a) A H-atom wave function has the following structure:

$$\psi_{nlm}(r, \theta, \phi) = \frac{1}{4\sqrt{2\pi}} \left( \frac{r}{a_0} \right)^{3/2} (2 - \sigma) e^{-\sigma/2} \cos \theta$$

(i) Find out the set of quantum number n, l, m for the state represented by the above wave function.

(ii) With the aid of qualitative plots show how the wave function, probability density and radial probability density changes with  $\sigma$  (scaled form of the distance of electron from the nucleus). [3+4]

- b) Write down the Schrodinger's equation (time independent form) for simple harmonic oscillator.

Show that the function  $\psi = \sqrt{2\alpha} \left( \frac{\alpha}{\pi} \right)^{1/4} x e^{-\alpha x^2/2}$  is a solution to it (x is the distance from the equilibrium position). Find out the corresponding energy eigenvalue. [2+3+2]

4. a) Consider the following wave functions :

$$\psi_{nlm}(r, \theta, \phi) = \frac{1}{\sqrt{64\pi}} \left(\frac{r}{a_0}\right)^{\frac{3}{2}} \sigma e^{-\frac{\sigma}{2}} \sin\theta e^{i\phi}$$

and

$$\psi_{nlm}(r, \theta, \phi) = \frac{1}{\sqrt{64\pi}} \left(\frac{r}{a_0}\right)^{\frac{3}{2}} \sigma e^{-\frac{\sigma}{2}} \sin\theta e^{-i\phi}$$

Construct a pair of real orbitals from these complex ones. Comment whether these newly constructed orbitals would give the same value for energy, angular momentum and z-component of angular momentum. [3+3]

- b) Calculate the zero point energy of a linear simple harmonic oscillator consisting of a particle of mass  $2.33 \times 10^{-26}$  kg and force constant  $155 \text{ Nm}^{-1}$ . [2]
- c) Calculate the value of classical turning point of a harmonic oscillator in the ground state in terms of frequency  $\nu$ . Is it possible to find a quantum oscillator outside this turning point? [3]
- d) The wave function of 1s orbital has the form,  $\psi_{1s}(r, \theta, \phi) = \frac{1}{\sqrt{\pi}} \left(\frac{r}{a_0}\right)^{\frac{3}{2}} e^{-\sigma}$ , find out the distance at which the radial probability is maximum. [3]

### Unit : III

[10 marks]

5. a) Conductance, specific conductance, equivalent conductance, equivalent conductance at infinite dilution : mention how each of these quantities depend on concentration? [4]
- b) A moving boundary experiment is done to measure the transference number of  $\text{Li}^+$  in 0.01 mol/L LiCl. In a tube having a cross sectional area of  $0.125 \text{ cm}^2$ , the boundary moves 7.3 cm in 1490 s using a current of  $1.80 \times 10^{-3}$  A. Calculate  $t_+$ . [3]
- c) Establish a relation between ion conductance and ionic mobility of an ion. [3]
6. a) Derive a relation that shows how the equivalent conductance of a weak electrolyte changes with concentration. Also mention how this equation helps to determine the dissociation constant of the weak electrolyte. [3+1]
- b) The specific conductance of a saturated solution of  $\text{BaSO}_4$  is  $3.48 \times 10^{-6} \text{ S/cm}$  and that of pure water is  $5 \times 10^{-7} \text{ S/cm}$ . The ionic conductance values of  $\text{Ba}^{2+}$  and  $\text{SO}_4^{2-}$  ions are 127.26 and  $160.04 \text{ S cm}^2/\text{mol}$ . Calculate the solubility product of  $\text{BaSO}_4$ . [3]
- c) The equivalent conductance of LiCl at infinite dilution is  $115.03 \times 10^{-4} \text{ S m}^2/\text{mol}$ . The cationic transport number is 0.336. Calculate the mobility of the cation and its velocity if the applied potential difference across two electrodes, 0.4 cm apart, is 6.0 volt. [3]

### Unit : IV

[12 marks]

7. a) If molar polarization of  $\text{NH}_3(\text{g})$  obeys equation  $P_m = a + b/T$ , where the constant a and b have the values 5.6 and  $12.000 \text{ cm}^3 \text{ mol}^{-1}$ , respectively, what is the relative permittivity of ammonia gas at STP? [ $P_m = \left(\frac{\epsilon_r - 1}{\epsilon_r + 2}\right) V_m$ ] [3]
- b) A cell is given as  $\text{Cd} | \text{Cd}^{2+} (a = 1) || \text{H}^+ (a = 1) | \text{H}_2 (1 \text{ atm}) | \text{Pt}$ , where displacement of  $\text{H}^+$  ions from solution occurs by Cd metal. Using standard condition, show that  $\Delta G^\circ$  is an extensive property, whereas  $E^\circ$  is an intensive property. [ $E_{\text{cell}} = 0.403 \text{ V}$  at  $25^\circ\text{C}$ ] [3]

- c) (i) Use Gibbs-Helmholtz equation to find out the expression of  $\Delta H$  in terms of temperature coefficient of EMF.  
(ii) For the cell,  $\text{Pb} | \text{PbCl}_2(\text{s}) | 0.1\text{N KCl} | \text{Hg}_2\text{Cl}_2(\text{s}) | \text{Hg}$ ,  $E_{\text{cell}} = 0.5356 \text{ V}$ . Write the cell reaction for 1F current. If the  $(\delta E/\delta T)_P = 1.45 \times 10^{-4}$ , find out the values of  $\Delta H$  and  $\Delta G$  for the same condition. [3+4+(2+3)]
8. a) If dipole moment of the monosubstituted benzene  $\text{C}_6\text{H}_5\text{X}$ , derive expressions for the 1,2-disubstituted benzene, and 1,4-disubstituted benzene, symbolically represented as  $\text{C}_6\text{H}_4\text{X}_2$ .
- b) Metallic Pb cannot displace  $\text{Sn}^{+2}$  ions from solution to form metallic Sn, at standard condition. What will happen, if Pb is placed in a solution with  $a_{\text{Sn}^{+2}} = 1.0$  gm ion  $\text{lit}^{-1}$  and that of  $a_{\text{Pb}^{+2}} = 0.1$  gm ion  $\text{lit}^{-1}$ ? Also write down the cell structure for the spontaneous process at this condition. [Given,  $E^0(\text{Pb}/\text{Pb}^{+2}) = 0.126 \text{ V}$  and  $E^0(\text{Sn}/\text{Sn}^{+2}) = 0.140 \text{ V}$ ]
- c) At  $25^\circ\text{C}$ , for the cell  $\text{Ag} | \text{AgCl}(\text{s}) | 0.1\text{N KCl} | \text{Hg}_2\text{Cl}_2(\text{s}) | \text{Hg}$ ,  $E_{\text{cell}} = 0.0455 \text{ V}$ . Calculate the activity (or concentration) of  $\text{Ag}^+$  in saturated solution of AgCl in 0.1 N KCl.
- d) Show that every 10 fold decrease in the ratio of activities or roughly concentrations, of the cations results in the oxidation potential becoming more +ve by  $0.0592/n \text{ V}$ , at  $25^\circ\text{C}$ . And further comment on the fact that a change from 1 gm ion to 0.1 gm ion per lit produces the same change as in decrease from  $10^{-6}$  to  $10^{-7}$  gm ion per lit. [3+3+2+4]

\_\_\_\_\_ × \_\_\_\_\_